1. *This question should be answered on the sheet provided.*

A College wants to connect the computerised registration equipment at its six sites, A to F. The table below shows the cost, in pounds, of connecting any two of the sites.

	A	B	C	D	E	F
A	–	130	190	155	140	125
B	130	–	215	200	190	170
C	190	215	–	110	180	100
D	155	200	110	–	70	45
E	140	190	180	70	–	75
F	125	170	100	45	75	–

Starting at D, use Prim's algorithm to find a minimum connector and draw the minimum spanning tree. Hence, state the lowest cost of connecting all the sites.

(5 marks)

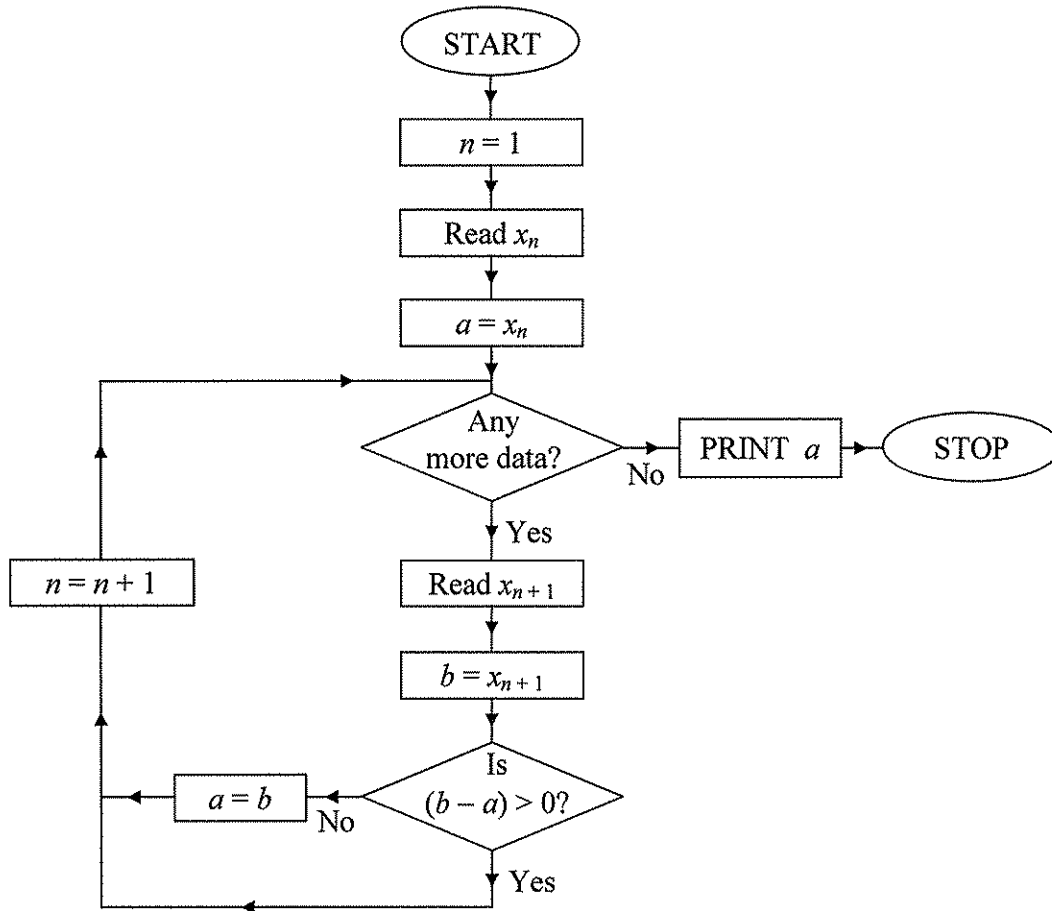**2.** *This question should be answered on the sheet provided.*

Fig. 1

The data

$$x_1 = 8, \quad x_2 = 2, \quad x_3 = 4, \quad x_4 = 3, \quad x_5 = 5, \quad x_6 = 1, \quad x_7 = 7,$$

is to be used in the algorithm given in Figure 1.

(a) Complete the table on the answer sheet recording the results of each instruction as the algorithm is applied and state the final output using the given data.

(6 marks)

(b) Explain what the algorithm achieves for any set of data x_1 to x_n. **(1 mark)**

5. A clothes manufacturer has a trademark "VE" which it wants to embroider on all its garments. The stitching must be done continuously but stitching along the same line twice is allowed.
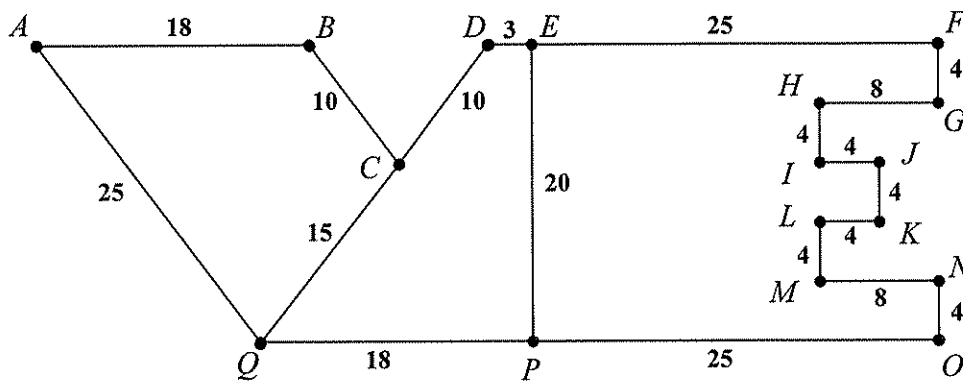
Logo 1:
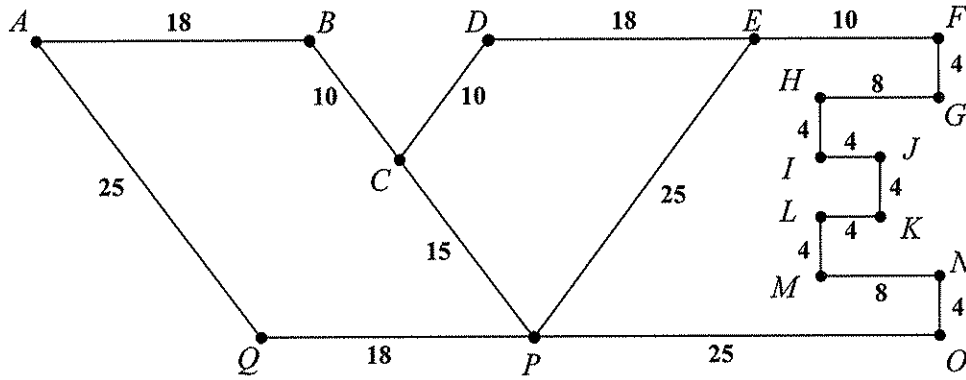
Logo 2:

Fig. 4

The weighted networks in Figure 4 represent two possible Logos.

The weights denote lengths in millimetres.

(a) Calculate the shortest length of stitch required to embroider Logo 1.　　　　**(4 marks)**

(b) Calculate the shortest length of stitch required to embroider Logo 2.　　　　**(6 marks)**

(c) Hence, determine the difference in the length of stitching required for the two Logos.

(1 mark)

6. A company makes lighting sets to be sold to stores for use during the Christmas period. As the product is only required at this time of year, all manufacturing takes place during September, October and November.

The sets are delivered to stores at the end of each of these months. Any sets that have been made but do not need to be delivered at the end of each of September and October are put into storage which the company must pay for.

Let x, y and z be the number of sets manufactured in September, October and November respectively.

The demand for lighting sets and the relevant costs are shown in the table below.

Month	September	October	November
Manufacturing costs per set during each month (£)	500	800	600
Demand for sets at the end of each month	800	1000	700
Cost of storing sets during each month (£)	–	100	150

The company must be able to meet the demand at the end of each month and there must be no unsold articles at the end of November.

(a) (i) Express z in terms of x and y.

   (ii) Hence, find an expression for the total costs incurred in terms of x and y.

(6 marks)

The company wishes to minimise its total costs by modelling this situation as a linear programming problem.

(b) Find as inequalities the constraints that apply in addition to $x \geq 800$ and $y \geq 0$.

(2 marks)

(c) On graph paper, illustrate these inequalities and label clearly the feasible region.

(4 marks)

(d) Use your graph to solve the problem. You must state how many sets should be produced in each month and the total costs incurred by the company.

(3 marks)

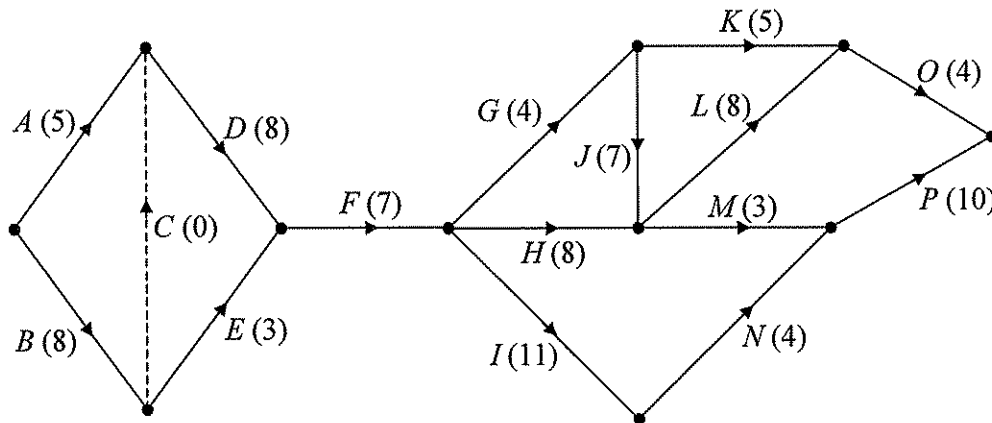*This question should be answered on the sheet provided.*

Fig. 5

The activity network in Figure 5 models the work involved in laying the foundations and putting in services for an industrial complex. The activities are represented by the arcs and the numbers in brackets give the time, in days, to complete each activity. Activity C is a dummy.

(a) Execute a forward scan to calculate the early times and a backward scan to calculate the late times, for each event.

(6 marks)

(b) Determine which activities lie on the critical path and list them in order. **(2 marks)**

(c) State the minimum length of time needed to complete the project. **(1 mark)**

The contractor is committed to completing the project in this minimum time and faces a penalty of £50 000 for each day that the project is late. Unfortunately, before any work has begun, flooding means that activity F will take 3 days longer than the 7 days allocated.

(d) Activity N could be completed in 1 day at an extra cost of £90 000. Explain why doing this is not economical.

(3 marks)

(e) If the time taken to complete any one activity, other than F, could be reduced by 2 days at an extra cost of £80 000, for which activities on their own would this be profitable. Explain your reasoning.

(3 marks)

END